

## Iterating with Numbers

### ► Loops

#### ► When to Use Loops

Many computations involve iterating over numbers:

- Checking each item in an array
- Computing sums or products from **0** to **n**

One way to write such loops:

**Step 1.** Set **i** to the starting number

**Step 2.** If **i** is too big, stop

Otherwise, do something with **i**

**Step 3.** Change **i** to the next value and go to **Step 2**

## For Loops

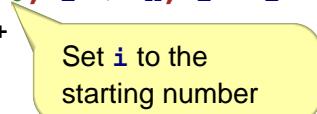
Java supports this pattern with **for**

```
int sum(int n) {  
    int res = 0;  
    for (int i = 0; i <= n; i = i + 1) {  
        res = res + i;  
    }  
    return res;  
}
```

## For Loops

Java supports this pattern with **for**

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int sum(int n) {  
    int res = 0;  
    for (int i = 0; i <= n; i = i + 1) {  
        res = res +  
    }  
    return res;  
}
```



Set **i** to the starting number

## For Loops

Java supports this pattern with `for`

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int sum(int n) {  
    int res = 0;  
    for (int i = 0; i <= n; i = i + 1) {  
        res = res + i;  
    }  
    return res;  
}
```

If `i` isn't too big...

## For Loops

Java supports this pattern with `for`

```
int sum(int n) {  
    int res = 0;  
    for (int i = 0; i <= n; i = i + 1) {  
        res = res + i;  
    }  
    return res;  
}
```

Do something with `i`

## For Loops

Java supports this pattern with `for`

```
int sum(int n) {  
    int res = 0;  
    for (int i = 0; i <= n; i = i + 1) {  
        res = res + i;  
    }  
    return res;  
}
```

Change `i` to the next value

## Another Example

```
int sumElements(int[] a) {  
    int res = 0;  
    for (int i = 0; i < a.length(); i = i + 1) {  
        res = res + a[i];  
    }  
    return res;  
}
```

## Another Example

```
int maxElement(int[] a) {
    int res = a[0];
    for (int i = 1; i < a.length(); i = i + 1) {
        if (res < a[i])
            res = a[i];
    }
    return res;
}
```

## Another Example

```
int isArrayMember(Object o, Object[] a) {
    for (int i = 0; i < a.length(); i = i + 1) {
        if (o.equals(a[i]))
            return true;
    }
    return false;
}
```

## Looping with Values Other than Numbers

With suitable methods and helpers, the same pattern can work for list-shaped data:

```
int isListMember(Object o, List lst) {
    for (Iterator e = lst.iterator();
         e.hasNext();
         )
    {
        Object elem = e.next();
        if (o.equals(elem))
            return true;
    }
    return false;
}
```

## While Loops

```
while (test) { ... }
```

is a shorthand for

```
for (; test; ) { ... }
```

```
int isListMember(Object o, List lst) {
    Iterator e = lst.iterator();
    while (e.hasNext()) {
        Object elem = e.next();
        if (o.equals(elem))
            return true;
    }
    return false;
}
```

## Do/While Loops

```
do { ... } while (test);
```

is a shorthand for

```
for (boolean ok=true; ok; ) { ... ok = test; }
```

```
int tryUntil(List lst, Tester t) {
    Enumerator e = lst.elements();
    do {
        Object elem = e.nextElement();
    } while (!t.tryIt(elem));
}
```

## When to Use Loops

Use **for**, **while** and **do** like you would use **filter** or **map**

- In other words, it's a question of reusing a pattern

Using **map** in Scheme is always optional, but sometimes you really *must* use **for** in Java

This is a design flaw in Java that you'll have to live with

As someone who knows how to design programs, you should understand

- why **for** is necessary
- how to convert recursive programs to use **for**

## ► Loops

### ► When to Use Loops

... and why Java needs a special form for loops

## Cost of Computation, Revisited

```
; sum : num -> num
; Sums the numbers from 0 to n
(define (sum n)
  (cond
    [(zero? n) 0]
    [else (+ n (sum (- n 1))))])
```

How long does (**sum** *n*) take?

$$\begin{aligned} T(0) &= k_1 \\ T(n) &= k_2 + T(n-1) \end{aligned}$$

So it takes  $k_1 + k_2 n$ , i.e., proportional to *n*

## Cost of Computation, Revisited

```
; sum : num -> num
; Sums the numbers from 0 to n
(define (sum n)
  (cond
    [(zero? n) 0]
    [else (+ n (sum (- n 1))))]))
```

How much *space* does `(sum n)` take?

```
(sum n)
→ → (+ n (sum n-1))
→ → (+ n (+ n-1 (sum n-2)))
→ → → (+ n (+ n-1 (+ n-2 ... 0)))
```

So it takes space proportional to  $n$

## Cost of Computation with an Accumulator

```
; asum : num num -> num
; Sums the numbers from 0 to n, added to res
(define (asum n res)
  (cond
    [(zero? n) res]
    [else (asum (- n 1) (+ res n))]))
```

How long does `(asum n 0)` take?

Still proportional to  $n$

## Cost of Computation with an Accumulator

```
; asum : num num -> num
; Sums the numbers from 0 to n, added to res
(define (asum n res)
  (cond
    [(zero? n) res]
    [else (asum (- n 1) (+ res n))]))
```

How much *space* does `(asum n 0)` take?

```
(asum n 0)
→ → (asum n-1 n)
→ → (asum n-2 2n-1)
→ → → (asum 0 n2/2+n/2)
```

So it takes constant space, independent of  $n$

## Time and Space

- Weeks ago, we saw how an accumulator can save lots of time
- Less frequently, an assuumulator can save space (sometimes even when it saves no time)

Accumulators save space when the result of a recursive call is the result for the current call:

```
(define (asum n res)
  (cond
    [(zero? n) res]
    [else (asum (- n 1) (+ res n))]))
```

As it turns out, recursive-call space in Java tends to be more scarce than other space, so this kind of saving is often important

## Cost of Computation in Java

```
class Summer {  
    int sum(int n) {  
        if (n == 0)  
            return 0;  
        else  
            return n+this.sum(n-1);  
    }  
}
```

How long does `new Summer.sum(n)` take?

Still proportional to  $n$

## Cost of Computation in Java

```
class Summer {  
    int sum(int n) {  
        if (n == 0)  
            return 0;  
        else  
            return n+this.sum(n-1);  
    }  
}
```

How much space does `new Summer.sum(n)` take?

```
s.sum(n)  
→ → return n+s.sum(n-1)  
→ → return n+(return n-1+s.sum(n-2))  
→ → → return n+(return n-1+(return n-2+...0))
```

Again, space proportional to  $n$

## Cost of Computation in Java

```
class Summer {  
    int asum(int n, int res) {  
        if (n == 0)  
            return res;  
        else  
            return this.asum(n-1, res+n);  
    }  
}
```

How long does `new Summer.asum(n, 0)` take?

Still proportional to  $n$

## Cost of Computation in Java

```
class Summer {  
    int asum(int n, int res) {  
        if (n == 0)  
            return res;  
        else  
            return this.asum(n-1, res+n);  
    }  
}
```

How much space does `new Summer.asum(n, 0)` take?

```
s.asum(n, 0)  
→ → return s.asum(n-1, n)  
→ → return return s.asum(n-2, 2n-1))  
→ → → return return ... return  $n^2/2+n/2$ 
```

Still space proportional to  $n$ , due to all the `returns`

## Tail Calls in Java

```
class Summer {
    int asum(int n, int res) {
        if (n == 0)
            return res;
        else
            return this.asum(n-1, res+n);
    }
}
```

The `return` explanation reflects the actual semantics of Java: redundant `returns` do not get dropped

- To allow constant-space loops, languages like Java provide a special form
- The special form only works for loops with no arguments

## Getting Rid of Arguments

```
(define (sum n)
  (local [(define (asum i res)
            (cond
              [(zero? i) res]
              [else (asum (- i 1) (+ res i))]))]
  (asum n 0)))
```

Equivalent Scheme code (in extremely poor style):

```
(define (sum n)
  (local [(define res 0)
          (define i n)
          (define (asum)
            (cond
              [(zero? i) (void)]
              [else (set! res (+ res i))
                    (set! i (- i 1))
                    (asum))])
          (asum)
          res)))
```

## Loops in Java

```
(define (sum n)
  (local
    [(define res 0)
     (define i n)
     (define (asum)
       (cond
         [(zero? i) (void)]
         [else (set! res (+ res i))
               (set! i (- i 1))
               (asum))])
     (asum)
     res)))
  class Summer {
    int sum(int n) {
      int res = 0;
      int i = n;
      while (true) {
        if (i == 0)
          break;
        else {
          res = res + i;
          i = i - 1;
        }
      }
      return res;
    }
}
```

The `while` form is like a recursive function that always either returns void or calls itself with no arguments

## Loops in Java, Slightly Better Style

```
while (true) { if (test) break; else ... }
⇒ while (test) { ... }

class Summer {
  int sum(int n) {
    int res = 0;
    int i = n;
    while (true) {
      if (i == 0)
        break;
      else {
        res = res + i;
        i = i - 1;
      }
    }
    return res;
  }
}

class Summer {
  int sum(int n) {
    int res = 0;
    int i = n;
    while (i == 0) {
      res = res + i;
      i = i - 1;
    }
    return res;
  }
}
```

## Loops in Java, Good Style

```
init; while (test) { ... incr; }
⇒ for (init; test; incr) { ... }

class Summer {
    int sum(int n) {
        int res = 0;
        int i = n;
        while (true) {
            if (i == 0)
                break;
            else {
                res = res + i;
                i = i - 1;
            }
        }
        return res;
    }
}
```

## When Loops Don't Work

Converting tree recursion into a loop usually won't work, because there are multiple recursive calls for each call

Some algorithms, such as [merge-sort](#), also involve multiple recursive calls

Technically, any program can be converted by manually creating [\*continuations\*](#), but that's a topic for CS 3520

## Loops in Java

Conclusion:

- Use [for](#) and [while](#) to make your code look and run better
- When in doubt, write the recursive version first