Lecture 17: Review Session



UofU ACM club kickoff!

Come join us for the re-launch of the flagship computing club at the U!



Just one Students are allowed to bring 3 A4/letter-sized sheets of paper with anything written/printed on both sides. In addition, you may bring the ``green sheet''. You may also bring a phone/calculator that can be used for any numeric calculations (but it's also ok to write a mathematical term, say 1.4/2.2 GHz without doing the calculation). You may of course not use your phone to surf the web or consult with others during the test. You may also not use the MARS simulator or other calculators/tools for numeric conversions. If necessary, make reasonable assumptions and clearly state them. The only clarifications you may ask for during the exam are definitions of terms. You will receive partial credit if you show your steps and explain your line of thinking, so attempt every question even if you can't fully solve it. Complete your answers in the space provided (including the back-side of each page). Confirm that you have 14 questions on 8 pages, followed by a blank page. Turn in your answer sheets before 10:35am. The test is worth 100 points and you have about 90 minutes, so allocate time cordingly.



Modern Trends

- Historical contributions to performance:
 - Better processes (faster devices) ~20%
 - Better circuits/pipelines ~15%
 - Better organization/architecture ~15%

Today, annual improvement is closer to 20%; this is primarily because of slowly increasing transistor count and more cores.

Need multi-thread parallelism and accelerators to boost performance every year.

Performance Measures

- Performance = 1 / execution time
- Speedup = ratio of performance
- Performance improvement = speedup -1
- Execution time = clock cycle time x CPI x number of instrs

Program takes 100 seconds on ProcA and 150 seconds on ProcB

Speedup of A over B = 150/100 = 1.5Performance improvement of A over B = 1.5 - 1 = 0.5 = 50%

Speedup of B over A = 100/150 = 0.66 (speedup less than 1 means performance went down) Performance improvement of B over A = 0.66 – 1 = -0.33 = -33% or Performance degradation of B, relative to A = 33%

If multiple programs are executed, the execution times are combined into a single number using AM, weighted AM, or GM CPU execution time = CPU clock cycles x Clock cycle time

CPU clock cycles = number of instrs x avg clock cycles per instruction (CPI)

Substituting in previous equation,

Execution time = clock cycle time x number of instrs x avg CPI

If a 2 GHz processor graduates an instruction every third cycle, how many instructions are there in a program that runs for 10 seconds?

- Dyn power α activity x capacitance x voltage² x frequency
- Capacitance per transistor and voltage are decreasing, but number of transistors and frequency are increasing at a faster rate
- Leakage power is also rising and will soon match dynamic power
- Power consumption is already around 100W in some high-performance processors today

• A 1 GHz processor takes 100 seconds to execute a CPU-bound program, while consuming 70 W of dynamic power and 30 W of leakage power. Does the program consume less energy in Turbo boost mode when the frequency is increased to 1.2 GHz?

Normal mode energy = 100 W x 100 s = 10,000 J Turbo mode energy = (70 x 1.2 + 30) x 100/1.2 = 9,500 J

Note:

Frequency only impacts dynamic power, not leakage power. We assume that the program's CPI is unchanged when frequency is changed, i.e., exec time varies linearly with cycle time.

Basic MIPS Instructions

- lw \$t1, 16(\$t2)
- add \$t3, \$t1, \$t2
- addi \$t3, \$t3, 16
- sw \$t3, 16(\$t2)
- beq \$t1, \$t2, 16
- blt is implemented as slt and bne
- j 64
- jr \$t1
- sll \$t1, \$t1, 2

Convert to assembly: while (save[i] == k) i += 1;

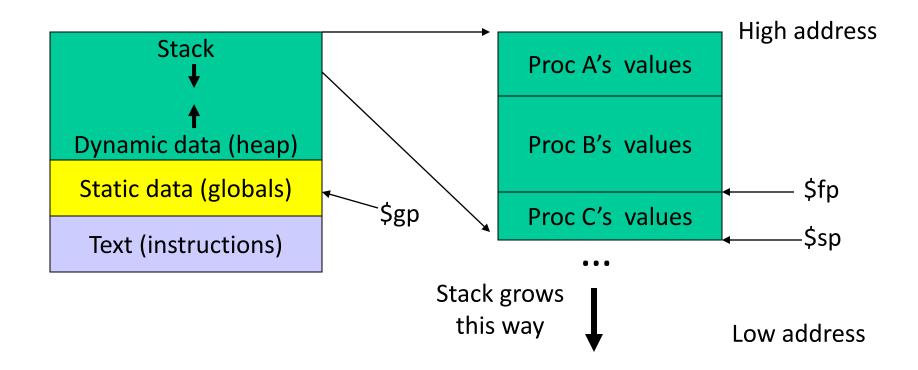
i and k are in \$s3 and \$s5 and base of array save[] is in \$s6

Loop:	sll	\$t1, \$s3, 2
	add	\$t1, \$t1, \$s6
	lw	\$t0, 0(\$t1)
	bne	\$t0, \$s5, Exit
	addi	\$s3, \$s3, 1
	j	Loop
Exit:		8

Registers

• The 32 MIPS registers are partitioned as follows:

 Register 0 : \$zero Regs 2-3 : \$v0, \$ Regs 4-7 : \$a0-\$ Regs 8-15 : \$t0-\$ Regs 16-23: \$s0-\$ Regs 24-25: \$t8-\$ 	 return values of a procedure input arguments to a procedure temporaries variables more temporaries
■ Reg 28 : \$gp	global pointer
Reg 29 : \$sp	stack pointer
Reg 30 : \$fp	frame pointer
■ Reg 31 :\$ra	return address



```
procA (int i)
{
    int j;
    j = ...;
    i = call procB(j);
    ... = i;
}
```

procA:

\$s0 = ... # value of j
\$t0 = ... # some tempval
\$a0 = \$s0 # the argument
...
jal procB
...
... = \$v0

procB (int j)
{
 int k;
 ... = j;
 k = ...;
 return k;
}

procB:

\$t0 = ... # some tempval ... = \$a0 # using the argument \$s0 = ... # value of k \$v0 = \$s0; jr \$ra

Saves and Restores

- Caller saves:
 - \$ra, \$a0, \$t0, \$fp (if reqd)
- Callee saves:

■ \$s0

As every element is saved on stack, the stack pointer is decremented

procA:

```
$s0 = ... # value of j
$t0 = ... # some tempval
$a0 = $s0 # the argument
...
jal procB
...
... = $v0
```

procB:

\$t0 = ... # some tempval ... = \$a0 # using the argument \$s0 = ... # value of k \$v0 = \$s0; jr \$ra

Example 2

```
int fact (int n)
```

```
if (n < 1) return (1);
else return (n * fact(n-1));
```

Notes:

{

The caller saves \$a0 and \$ra in its stack space. Temps are never saved.

```
fact:
       $sp, $sp, -8
 addi
  sw $ra, 4($sp)
 sw $a0, 0($sp)
 slti $t0, $a0, 1
  beq $t0, $zero, L1
 addi $v0, $zero, 1
 addi $sp, $sp, 8
 jr
       $ra
L1:
       $a0, $a0, -1
 addi
 jal
        fact
       $a0, 0($sp)
  lw
  lw $ra, 4($sp)
 addi $sp, $sp, 8
       $v0, $a0, $v0
 mul
 jr
        $ra
```

- Decimal $35_{10} = 3 \times 10^1 + 5 \times 10^0$
- Binary $00100011_2 = 1 \times 2^5 + 1 \times 2^1 + 1 \times 2^0$
- Hexadecimal (compact representation) 0x 23 or $23_{hex} = 2 \times 16^1 + 3 \times 16^0$

0-15 (decimal) \rightarrow 0-9, a-f (hex)

Dec	Binary	Hex									
0	0000	00	4	0100	04	8	1000	08	12	1100	0 c
1	0001	01	5	0101	05	9	1001	09	13	1101	0d
2	0010	02	6	0110	06	10	1010	0a	14	1110	0 e
3	0011	03	7	0111	07	11	1011	0b	15	1111	Of
											14

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2's Complement

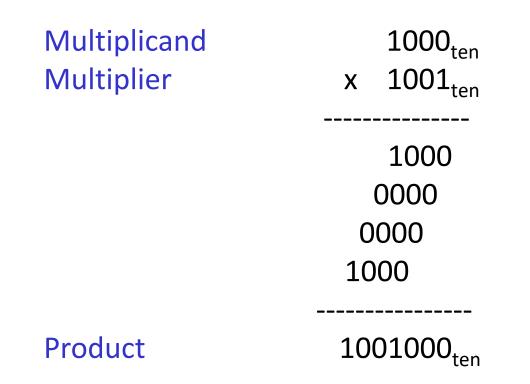
```
\begin{array}{l} 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0001_{two} = 0_{ten} \\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0001_{two} = 1_{ten} \\ ... \\ 0111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ two = 2^{31} - 1 \\ 1000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ two = -2^{31} \\ 1000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0001\ two = -(2^{31} - 1) \\ 1000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0010\ two = -(2^{31} - 1) \\ 1000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0010\ two = -(2^{31} - 2) \\ ... \\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ 1111\ two = -1 \end{array}
```

Note that the sum of a number x and its inverted representation x' always equals a string of 1s (-1).

$$x + x' = -1$$
 $x' + 1 = -x$ $-x = x' + 1$... hence, can compute the negative of a number byinverting all bits and adding 1

This format can directly undergo addition without any conversions! Each number represents the quantity

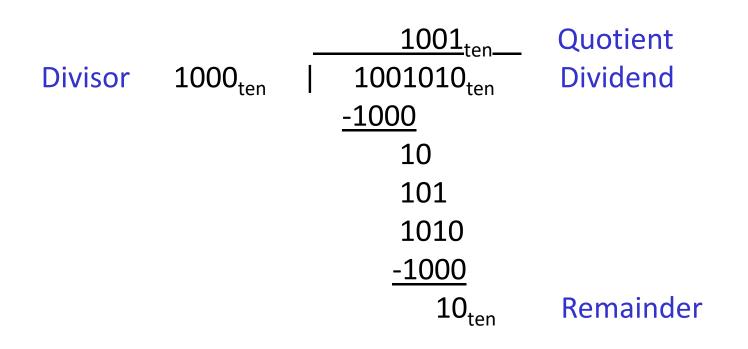
 $x_{31} - 2^{31} + x_{30} 2^{30} + x_{29} 2^{29} + ... + x_1 2^1 + x_0 2^0$



In every step

- multiplicand is shifted
- next bit of multiplier is examined (also a shifting step)
- if this bit is 1, shifted multiplicand is added to the product

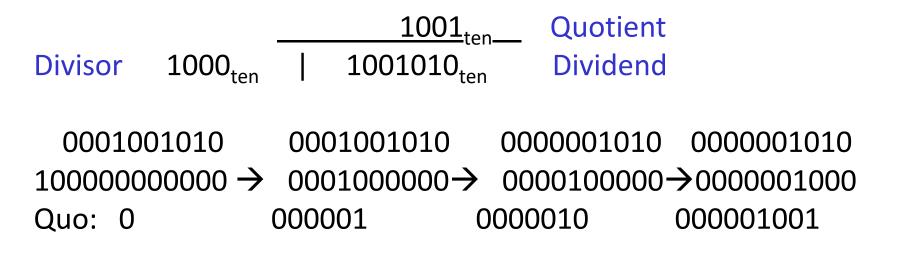
Division



At every step,

- shift divisor right and compare it with current dividend
- if divisor is larger, shift 0 as the next bit of the quotient
- if divisor is smaller, subtract to get new dividend and shift 1 as the next bit of the quotient

Division



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- 20.45 decimal = ? Binary
- 20 decimal = 10100 binary
- 0.45 x 2 = 0.9 (not greater than 1, first bit after binary point is 0)
 0.90 x 2 = 1.8 (greater than 1, second bit is 1, subtract 1 from 1.8)
 0.80 x 2 = 1.6 (greater than 1, third bit is 1, subtract 1 from 1.6)
 0.60 x 2 = 1.2 (greater than 1, fourth bit is 1, subtract 1 from 1.2)
 0.20 x 2 = 0.4 (less than 1, fifth bit is 0)
 0.40 x 2 = 0.8 (less than 1, sixth bit is 0)
 0.80 x 2 = 1.6 (greater than 1, seventh bit is 1, subtract 1 from 1.6)

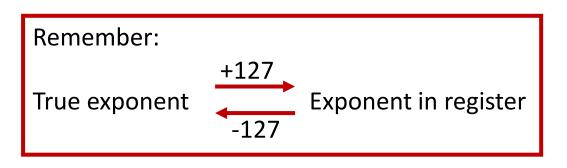
... and the pattern repeats

```
10100.01110011001100...
Normalized form = 1.0100011100110011... x 2<sup>4</sup>
```

• Represent -0.75_{ten} in single and double-precision formats

Single: (1 + 8 + 23)

Double: (1 + 11 + 52)



- What decimal number is represented by the following single-precision number?
 - 1 1000 0001 01000...0000

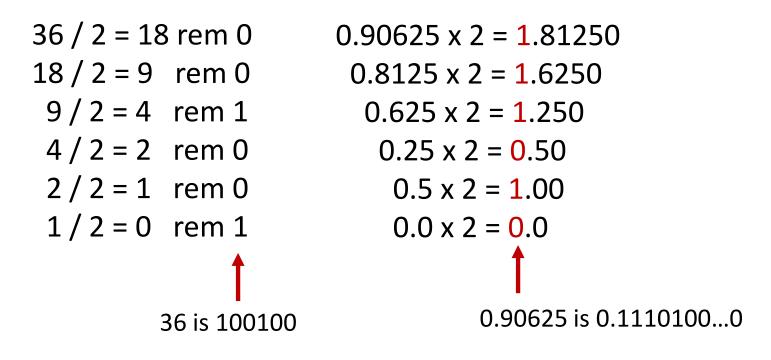
• Represent -0.75_{ten} in single and double-precision formats

```
Single: (1 + 8 + 23)
1 0111 1110 1000...000
```

```
Double: (1 + 11 + 52)
1 0111 1111 110 1000...000
```

- What decimal number is represented by the following single-precision number?
 - $1 \quad 1000 \ 0001 \quad 01000...0000$

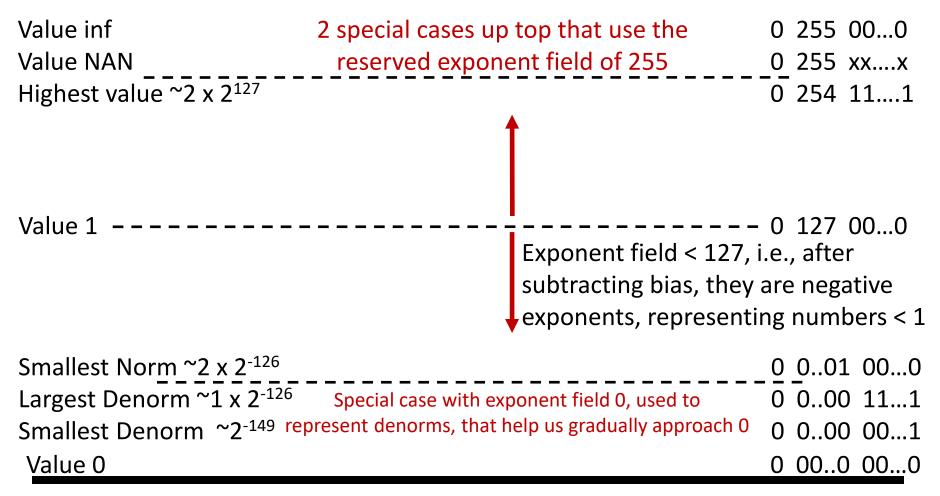
• Represent 36.90625_{ten} in single-precision format



We've calculated that $36.90625_{ten} = 100100.1110100...0$ in binary Normalized form = 1.001001110100...0 x 2⁵ (had to shift 5 places to get only one bit left of the point)

The sign bit is 0 (positive number) The fraction field is 001001110100...0 (the 23 bits after the point) The exponent field is 5 + 127 (have to add the bias) = 132, which in binary is 10000100

The IEEE 754 format is 0 10000100 001001110100.....0 sign exponent 23 fraction bits



Same rules as above, but the sign bit is 1 Same magnitudes as above, but negative numbers Consider the following binary example

```
1.010 \times 2^{1} + 1.100 \times 2^{3}
Convert to the larger exponent:
0.0101 \times 2^3 + 1.1000 \times 2^3
Add
1.1101 x 2<sup>3</sup>
Normalize
1.1101 x 2<sup>3</sup>
Check for overflow/underflow
Round
Re-normalize
```

Boolean Algebra

•
$$A + B = A \cdot B$$

•
$$A \cdot B = A + B$$

Α	В	С	E
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

Any truth table can be expressed as a sum of products

$(A \cdot B \cdot \overline{C}) + (A \cdot C \cdot \overline{B}) + (C \cdot B \cdot \overline{A})$

- Can also use "product of sums"
- Any equation can be implemented with an array of ANDs, followed by an array of ORs

- Ripple-Carry adder each 1-bit adder feeds its carry-out to next stage simple design, but we must wait for the carry to propagate thru all bits
- Carry-Lookahead adder each bit can be represented by an equation that only involves input bits (a_i, b_i) and initial carry-in (c₀) -- this is a complex equation, so it's broken into sub-parts

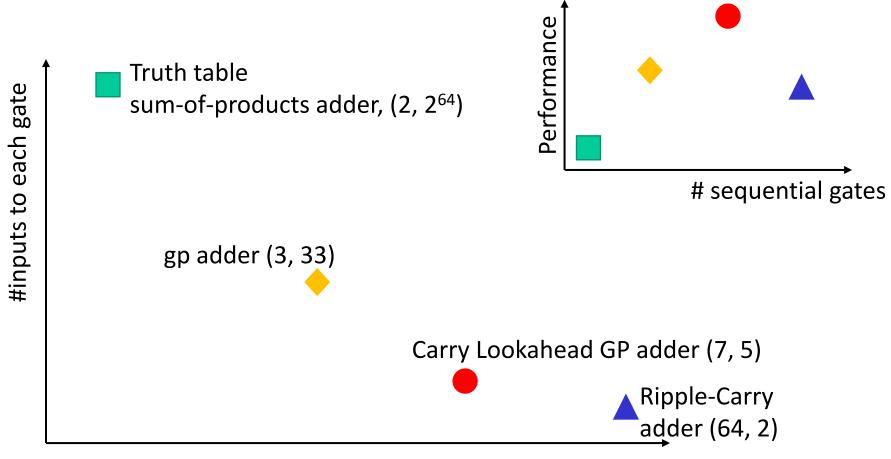
```
For bits a_i, b_i, and c_i, a carry is generated if a_i \cdot b_i = 1 and a carry is propagated if a_i + b_i = 1
C_{i+1} = g_i + p_i \cdot C_i
```

Similarly, compute these values for a block of 4 bits, then for a block of 16 bits, then for a block of 64 bits....Finally, the carry-out for the 64th bit is represented by an equation such as this:

$$C_4 = G_3 + G_2 \cdot P_3 + G_1 \cdot P_2 \cdot P_3 + G_0 \cdot P_1 \cdot P_2 \cdot P_3 + C_0 \cdot P_0 \cdot P_1 \cdot P_2 \cdot P_3$$

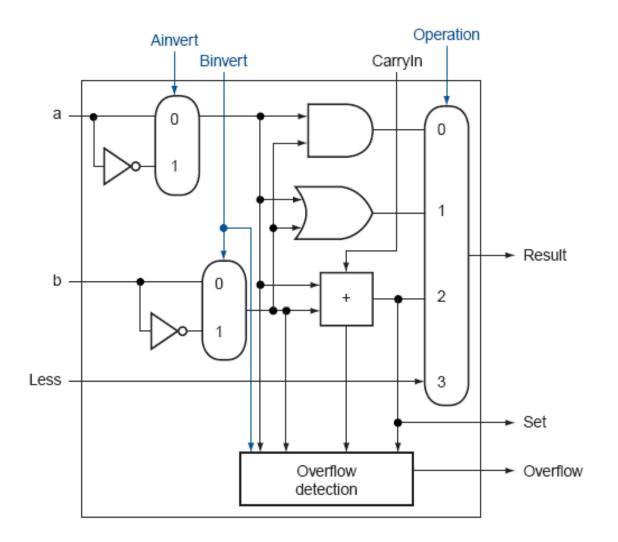
Each of the sub-terms is also a similar expression

Trade-Off Curve



sequential gates

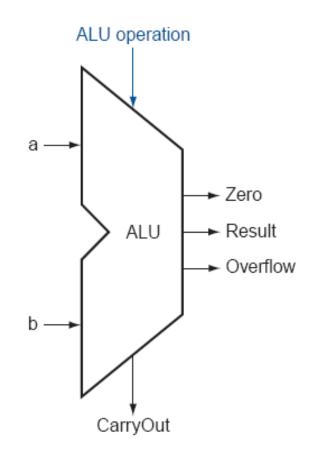
32-bit ALU



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What are the values of the control lines and what operations do they correspond to?

	Ai	Bn	Ор
AND	0	0	00
OR	0	0	01
Add	0	0	10
Sub	0	1	10
NOR	1	1	00
NAND	1	1	01
SLT	0	1	11
BEQ	0	1	10 (xx)



- Three questions worth asking:
 - What are the possible output states? Draw a bubble for each.
 - What are inputs? What values can those inputs take?
 - For each state, what do I do for each possible input value? Draw an arc out of every bubble for every input value.

Example – Residential Thermostat

- Two temp sensors: internal and external
- If internal temp is within 1 degree of desired, don't change setting
- If internal temp is > 1 degree higher than desired, turn AC on; if internal temp is < 1 degree lower than desired, turn heater on
- If external temp and desired temp are within 5 degrees, disregard the internal temp, and turn both AC and heater off

Finite State Machine Table

Current State	Input E	Input I	Output State
HEAT	D	С	OFF
HEAT	D	G	OFF
HEAT	D	Н	OFF
HEAT	U	С	HEAT
HEAT	U	G	HEAT
HEAT	U	Н	COOL
COOL	D	С	OFF
COOL	D	G	OFF
COOL	D	Η	OFF
COOL	U	С	HEAT
COOL	U	G	COOL
COOL	U	Н	COOL
OFF	D	С	OFF
OFF	D	G	OFF
OFF	D	Η	OFF
OFF	U	С	HEAT
OFF	U	G	OFF
OFF	U	Н	COOL
			1

Finite State Diagram

